Search Direction Generation via a Proposed Model

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Article Info Page Number: 138 – 141 Publication Issue: Vol 71 No. 1 (2022)

Article History

Article Received: 18 November 2021 Revised: 03 December 2021 Accepted: 19 December 2021 Publication: 28 January 2022

Abstract

This study proposes a decomposition method through which they can be a successful solution to multi-stage stochastic nonlinear programs. The proposed method entails the scenario analysis method. The proposed method also performs its role via search direction generation in such a way that sets of quadratic programming sub-issues are solved in a parallel way, especially when the size is significant lower, compared to the case involving original problems at the respective iterations. Relative to the dual multiplier derivation, which focuses on nonanticipativity constraints, the proposed system advocates for the introduction of generalized reduced gradient approaches. This study's focus is on the efforts seeking to establish a nonlinear programming model targeting problems with much nonlinearity, as well as linear constraints existing in large sparse sets; with the objective function on the focus. From experience, most of the linear programming issues are large (inordinately) because of their attempt towards approximation via piecewise linearization, translating into nonlinear issues. Also, most of the problems in the real-world have fewer variables linked to the objective function's nonlinearity.

Keywords: - SNLP, PHA etc.

Introduction

For optimization problems, one of the aspects representing or depicting a critical class entails stochastic nonlinear programming (SNLP) problems. These problems are ever-existing in the real-world scenarios. Also, most of the existing systems remain nonlinear inherently, pointing to the criticality of employing non-linear frameworks towards representing the systems, as well as the optimization of such systems by using nonlinear programming approaches. Another critical attribute to acknowledge is the uncertainty concept. In most cases, details of the systems under implementation are not known with precision and accuracy. Rather, variables and parameters are discerned relative to issues such as the ranges in which they occur or represent, as well as states of probability distributions. Given such scenarios, it is important to note that optimization can be realized via the incorporation of stochastic programming frameworks. Indeed, the emergence of the problems of multi-stage stochastic programming is felt and well-documented in practical scenarios, including portfolio selections and manpower and production planning.

Vol. 71 No. 1 (2022) http://philstat.org.ph In this case, the deterministic vector is represented by $Q_T = 0$. $x \in \Re^{n_o}$, te random vector realization $\hat{\xi}_i$, and the i-th stage decision vector ξ_i . $y_i \in \Re^{n_i}$, whose generations occur recursively through $x, y_1, ..., y_{i-1}$ and $\hat{\xi}_1, ..., \hat{\xi}_i$. Given \Re^{n_o} and its associated real-valued functions in the form of \hat{c}_o and c_o , were have $y_i(x, y_1, ..., y_{i-1}, \hat{\xi}_1, ..., \hat{\xi}_i)$. With a correlation between c_t and $\hat{\xi}_1, ..., \hat{\xi}_t$ documented, the form remains random.

Methodology

Given $\xi = (\xi_1, ..., \xi_{T-1})$ as a discrete random vector, should $c_{it}(i=1,...,S_t)$ be the infinite realizations of c_t , then on stage t, constraint functions become c_{ti} .

In [1], a comprehensive description regarding multi-stage stochastic program establishment is provided.

The introduction of the scenario analysis approach has been informed by the need to ensure that multi-stage stochastic programs are handled, an example of such a study being [2]. This approach focuses on a scenario's finite number with time. Given $\xi = (\xi_1, ..., \xi_{T-1})$ and the central assumption ebing that the associated space of probability is (Ω, θ, P) , if $\xi^{(s)} = (\xi_1^{(s)}, \xi_2^{(s)}, ..., \xi_{T-1})$ is the scenario at hand, with the probability distribution known and fixed, then it is possible to reformulate.

Results and Discussion

In situations where the scenario S is large, it is worth indicating that (5)-(7) also tend to be large, proving difficult to solve directly through techniques of general-purpose optimization. The eventuality is that decomposition methods have been established in a quest to address this gap, seeking to solve stochastic programming issues [3]. Additionally, computer parallelization has proved insightful and critical relative to feasible implementations of decomposition approaches. It is also notable that many studies have examined this area [4-7], which concerns nonlinear and linear programming. For the majority, they have focused on renowned decomposition guidelines [8], as well as the augmented Lagrangian function and Lagrangian-based duality theory. One of the efficient approaches involves the L-shaped decomposition technique, aiding in solving multi-stage stochastic linear issues. In the respective cycles, there is a recursive generation of optimal and feasible cut sets, causing a reduction in feasible regions. Other studies have documented other approaches [9, 10], including the logarithmic barrier approach, through which the programs could be solved and, in turn, steer system optimization. Given that all the methods rely on stochastic linear programs' special properties and structures, it is imperative to highlight that the generalization of the methods towards solving stochastic nonlinear programs is difficult.

With the scenario analysis approach employed [2], an iterative algorithm has been proposed in the form of the PHA (progressive hedging method). Also, this method has been applied towards stochastic generalized network solutions [10], with findings demonstrating satisfactory numerical observations. Other studies that have implemented the PHA technique [4, 5] contend that its challenge involves how to select a proper penalty variable. Hence, it has been affirmed not to be the best approach for application in loosely-coupled scenario analysis issues. In response, studies have proposed the bundle-based decomposition technique [6], which has been observed to be superior, compared to PHA. More recently, a newer approach has been

proposed [7], capable of addressing non-anticipativity constraints using a Lagrangian dual method, as well as combining logarithmic barrier techniques. Indeed, this method's implementation is ongoing.

This study's focus is on the efforts seeking to establish a nonlinear programming model targeting problems with much nonlinearity, as well as linear constraints existing in large sparse sets; with the objective function on the focus. From experience, most of the linear programming issues are large (inordinately) because of their attempt towards approximation via piecewise linearization, translating into nonlinear issues. Also, most of the problems in the real-world have fewer variables linked to the objective function's nonlinearity. In this case, x^N and x^L , which are linear portions, are achieved via the partitioning of x. Nonlinear variables, in this case, are represented by x^N , with A and c affecting all variables. In some situations, x^N in $c^T x$ could be introduced in $/(x^N)$. In other scenarios, c becomes 0. The central assumption in this case is that $/(x^N)$, given a feasible zone with gradient, could be differentiated continuously. Another assumption at this stage is that at any feasible point, represented by x^N , indeed, / and g can be computed. The eventual model is similar to the reduced-gradient approach [8], as well as the variable-reduction technique, observations drawn from the assertions by Gill and Murray [9]. This model could also been seen to extend the work of [2], who focused on the revised simplex approach.

Conclusion

When x and F(x) are partitioned to achieve nonlinear and linear terms, descriptive procedures can be realized. However, through /(x) and g(x), F(x) and VF(x) can be denoted easily.

In this case, matrices are expected to involve upper case letters while vectors are represented using lower case letters. For scalars presented in Greek, they are presented via lower-case letters. Thus, e > 0 is the floating-point arithmetic's precision.

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